

TYJ- 01 R MATHEMATICS SOLUTION 11 OCTOBER 2019

31. (c) Given lines are $2x - y + 7 = 0$ and $2x - y + 5 = 0$

Both the lines are on same side of origin.

$$\text{Distance between two parallel lines} = \frac{7-5}{\sqrt{2^2+1^2}} = \frac{2}{\sqrt{5}}$$

32. (b) $L \equiv 3x - 4y - 8 = 0$

$$L_{(3,4)} = 9 - 16 - 8 < 0 \text{ and } L_{(2,-6)} = 6 + 24 - 8 > 0$$

Hence, the points lie on different side of the line.

33. (a) It is given that the lines $ax + 2y + 1 = 0$, $bx + 3y + 1 = 0$ and $cx + 4y + 1 = 0$ are concurrent, therefore

$$\begin{vmatrix} a & 2 & 1 \\ b & 3 & 1 \\ c & 4 & 1 \end{vmatrix} = 0$$

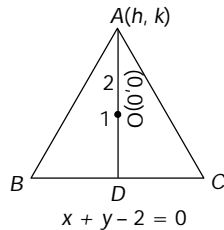
$$\Rightarrow -a + 2b - c = 0 \Rightarrow 2b = a + c$$

$\Rightarrow a, b, c$ are in A. P.

34. (b) $-y + 3x + 4 = 0$ and perpendicular is $\frac{y-3}{x-2} = \frac{-1}{3}$ or $3y + x - 11 = 0$. Therefore foot is $x = \frac{-1}{10}, y = \frac{37}{10}$.

35. (c) Let the co-ordinate of vertex A be (h, k) . Then AD is perpendicular to BC, therefore $OA \perp BC$

$$\Rightarrow \frac{k-0}{h-0} \times \frac{-1}{1} = -1 \Rightarrow k = h \quad \dots(i)$$



Let the coordinates of D be (α, β) . Then the co-ordinates of O are $\left(\frac{2\alpha+h}{2+1}, \frac{2\beta+k}{2+1}\right)$. Therefore

$$\frac{2\alpha+h}{3} = 0 \text{ and } \frac{2\beta+k}{3} = 0 \Rightarrow \alpha = -\frac{h}{2}, \beta = \frac{-k}{2}$$

Since (α, β) lies on $x + y - 2 = 0 \Rightarrow \alpha + \beta - 2 = 0$

$$\Rightarrow -h/2 - k/2 - 2 = 0 \Rightarrow h + k + 4 = 0$$

$$\Rightarrow 2h + 4 = 0 \Rightarrow h = k = -2, \quad [\text{from (i)}]$$

Hence the coordinates of vertex A are $(-2, -2)$.

36. (a) Equation of the line passing through $(3, 8)$ and perpendicular to $x + 3y - 7 = 0$ is $3x - y - 1 = 0$. The intersection point of both the lines is $(1, 2)$.

Now let the image of $A(3, 8)$ be $A'(x_1, y_1)$, then point $(1, 2)$ will be the mid point of AA' .

$$\Rightarrow \frac{x_1+3}{2} = 1 \Rightarrow x_1 = -1 \text{ and } \frac{y_1+8}{2} = 2 \Rightarrow y_1 = -4.$$

Hence the image is $(-1, -4)$.

37. (b) Let the co-ordinates of the third vertex be $(2a, t)$.

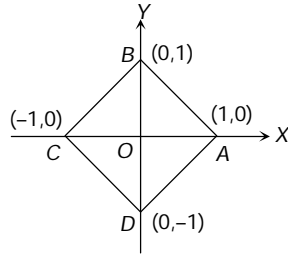
$$AC = BC \Rightarrow t = \sqrt{4a^2 + (a-t)^2} \Rightarrow t = \frac{5a}{2}$$

So the coordinates of third vertex C are $\left(2a, \frac{5a}{2}\right)$

Therefore area of the triangle

$$= \pm \frac{1}{2} \begin{vmatrix} 2a & \frac{5a}{2} & 1 \\ 2a & 0 & 1 \\ 0 & a & 1 \end{vmatrix} = \begin{vmatrix} a & \frac{5a}{2} & 1 \\ 0 & -\frac{5a}{2} & 0 \\ 0 & a & 1 \end{vmatrix} = \frac{5a^2}{2} \text{ sq. units.}$$

38. (a) Required locus of the point (x, y) is the curve $|x| + |y| = 1$. If the point lies in the first quadrant, then $x > 0, y > 0$ and so $|x| + |y| = 1 \Rightarrow x + y = 1$, which is straight line AB. If the point (x, y) lies in second quadrant then $x < 0, y > 0$ and so $|x| + |y| = 1 \Rightarrow -x + y = 1$



Similarly for third and fourth quadrant, the equations are $-x - y = 1$ and $x - y = 1$. Hence the required locus is the curve consisting of the sides of the square ABCD.

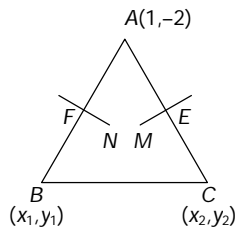
39. (c) According to question, $x_1 = \frac{2+4+x}{3} \Rightarrow x = 3x_1 - 6$

$$y_1 = \frac{5-11+y}{3} \Rightarrow y = 3y_1 + 6$$

$$\therefore 9(3x_1 - 6) + 7(3y_1 + 6) + 4 = 0$$

Hence locus is $27x + 21y - 8 = 0$, which is parallel to $9x + 7y + 4 = 0$.

40. (d) Let the equation of perpendicular bisector FN of AB is $x - y + 5 = 0$ (i)



The middle point F of AB is $\left(\frac{x_1 + 1}{2}, \frac{y_1 - 2}{2}\right)$ lies on line (i). Therefore $x_1 - y_1 = -13$

.....(ii)

Also AB is perpendicular to FN. So the product of their slopes is -1.

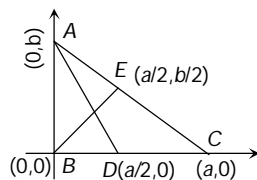
$$\text{i.e. } \frac{y_1 + 2}{x_1 - 1} \times 1 = -1 \text{ or } x_1 + y_1 = -1 \quad \text{.....(iii)}$$

On solving (ii) and (iii), we get $B(-7, 6)$.

Similarly $C\left(\frac{11}{5}, \frac{2}{5}\right)$.

Hence the equation of BC is $14x + 23y - 40 = 0$.

41. (c) From figure,



$$\left(\frac{b/2}{a/2}\right) \left(\frac{b}{-a/2}\right) = -1 \Rightarrow a^2 = 2b^2 \Rightarrow a = \pm\sqrt{2}b.$$

42. (c) Any line through $(1, -10)$ is given by $y + 10 = m(x - 1)$

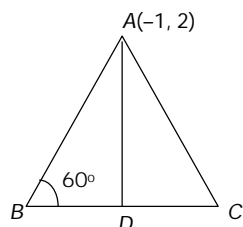
Since it makes equal angle say ' α ' with the given lines $7x - y + 3 = 0$ and $x + y - 3 = 0$, therefore

$$\tan \alpha = \frac{m-7}{1+7m} = \frac{m-(-1)}{1+m(-1)} \Rightarrow m = \frac{1}{3} \text{ or } -3$$

Hence the two possible equations of third side are $3x + y + 7 = 0$ and $x - 3y - 31 = 0$.

43. (a) $AD = \left| \frac{-2-2-1}{\sqrt{(2)^2 + (-1)^2}} \right| = \left| \frac{-5}{\sqrt{5}} \right| = \sqrt{5}$

$$\therefore \tan 60^\circ = \frac{AD}{BD} \Rightarrow \sqrt{3} = \frac{\sqrt{5}}{BD} \Rightarrow BD = \frac{\sqrt{5}}{\sqrt{3}}$$



$$\therefore BC = 2BD = 2 \cdot \frac{\sqrt{5}}{\sqrt{3}} = \sqrt{\frac{20}{3}}$$

44. (d) $m_1 = -1/3$ and $m_2 = 3$. Hence lines $x + 3y = 4$ and $6x - 2y = 7$ are perpendicular to each other.

Therefore the parallelogram is rhombus.

45. (b) Area of the right angled triangle is

$$= \frac{1}{2} (\text{Perpendicular}) \times (\text{base}) = \frac{1}{2} ab$$